Trapping of Neutral Mercury Atoms and Prospects for Optical Lattice Clocks

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(Received 16 October 2007; revised manuscript received 28 November 2007; published 8 February 2008)

We report vapor-cell magneto-optical trapping of Hg isotopes on the 1S0→3P1 intercombination transition. Six abundant isotopes, including four bosons and two fermions, were trapped. Hg is the heaviest nonradioactive atom trapped so far, which enables sensitive atomic searches for “new physics” beyond the standard model. We propose an accurate optical lattice clock based on Hg and evaluate its systematic accuracy to be better than 10−18. Highly accurate and stable Hg-based clocks will provide a new avenue for the research of optical lattice clocks and the time variation of the fine-structure constant.

DOI: 10.1103/PhysRevLett.100.053001 PACS numbers: 37.10.Gh, 06.30.Ft, 31.15.Vh

Precision tests of fundamental symmetries with atoms and molecules play an important role in probing new physics beyond the standard model of elementary particles. The “new physics” sensitivity of such experiments depends steeply on the nuclear charge Z of the atom. In particular, parity-violating amplitudes change as Z³ [1], atomic CP-violating (T-, P-odd) permanent electric dipole moments (EDM), as Z⁴ [2], and CP-violating polarizabilities, as Z⁵ [3]. As a result, the most accurate limit to date on the atomic EDM has been set with Hg atoms (Z = 80) and on the electron EDM with Ti (Z = 81) atoms [4,5]. In a quest for more sensitive probes, experiments with heavier atoms, Fr (Z = 87) and Ra (Z = 88), have been proposed [6,7]. However, all the elements with Z > 83 are radioactive and consequently experience associated drawbacks.

In this Letter, we report the vapor-cell magneto-optical trapping (MOT) of Hg isotopes and discuss its application to accurate optical lattice clocks [8]. Located at the very edge of the stability valley, Hg is, so far, the heaviest nonradioactive atom that has been laser-cooled and trapped. It is anticipated that these ultracold heavy atoms will enable experimental searches of high-Z atom physics with unprecedented sensitivity due to reduced motional effects, longer interrogation time, and higher optical thickness. Moreover, as demonstrated for Yb isotopes [9], a remarkable variety of trapped Hg isotopes (4 bosonic and 2 fermionic ones) may allow attaining Bose or Fermi degeneracy, which would further improve the measurements’ sensitivity.

We systematically evaluate various sources of uncertainty for the Hg-based optical lattice clock and argue that an accuracy of better than 10−18 is attainable, which is an order of magnitude of improvement over Sr [8] or Yb-based [10] clocks because of reduced susceptibility to the blackbody radiation field, which sets a major limitation on the accuracy of atomic clocks [10,11]. This projected accuracy is competitive with that of the best ion clock with Al⁺ [11]. In particular, we take advantage of the high nuclear charge Z of Hg to explore the variation of the fine-structure constant α that generically controls the strength of relativistic effects in the atom as (αZ)². While astrophysical observations suggest that α may drift at the rate of dα/α = 10⁻¹⁶ yr⁻¹ [12], recent laboratory tests based on the frequency ratio of accurate ion clocks and Cs clocks set the upper bound of |dα/α| < 1.3 × 10⁻¹⁶ yr⁻¹ [13] limited by the Cs clock’s inaccuracy of 1 × 10⁻¹⁵. Significant enhancement in measurement precision will be expected for direct comparison of optical clocks with the frequency comb technique [14]: the frequency change δν of Hg-based clocks operated at ν0 can be measured in reference to Sr [15] or Hg⁺ [13] clocks, where Hg, Sr, and Hg⁺ have sensitivity (δν/ν0)/(δα/α) of 0.81, 0.06, and −3.19, respectively, to the fractional change of dα/α [12,16].

The laser cooling and clockwork with neutral Hg exploit its divalent electronic structure and parallel techniques developed for Sr [8,17]. The energy levels of Hg are shown in Fig. 1. The spin-forbidden 1S₀→3P₁ transition at 253.7 nm with the natural linewidth of γ/2π = 1.3 MHz [18] provides an adequate cooling transition down to the Doppler temperature of 31 μK. The 1S₀→3P₀ transition at 265.6 nm, which is weakly allowed for odd isotopes with a nuclear spin (I ≠ 0) or even isotopes (I = 0) dressed by external fields [19,20], will be exploited as a clock transition. The magic wavelength, where the light-shift perturbations of the clock levels are canceled out [8,21], is calculated to be λₘ = 360 nm, as discussed later.
Trapping neutral Hg is experimentally challenging due to limited laser power available at deep-UV cooling transition wavelength. To overcome this difficulty and take advantage of its heavy mass and the large radiation pressure at the shorter wavelengths, we used a vapor-cell MOT [22] to capture the atoms from the low-velocity tail of the Maxwell-Boltzmann distribution. Our apparatus is shown in Fig. 2. Laser radiation at 253.7 nm was generated by frequency quadrupling a laser diode system operated at 1014.9 nm. The master laser was an external-cavity laser diode locked to a reference cavity to reduce its linewidth to less than 100 kHz. This master laser was amplified by a tapered amplifier up to 1 W and injected into a bow-tie cavity with a periodically poled lithium niobate crystal to generate 240 mW at 507.4 nm. This was further frequency doubled by a beta–barium borate crystal to obtain roughly 10 mW at 253.7 nm.

This UV light was fed into a vacuum chamber with a base pressure of $3 \times 10^{-10}$ Torr to form a vapor-cell MOT with a folded beam configuration with a single stroke. The $1/e^2$ diameter of the trapping beam was 20 mm with a power density of 0.3$I_0$, where $I_0 = 10$ mW/cm$^2$ is the saturation intensity of the $^1S_0 - ^3P_1$ transition. After introducing Hg, the vacuum pressure increased to $8 \times 10^{-9}$ Torr that indicated the Hg-atom number density of $7 \times 10^7$ cm$^{-3}$. The typical magnetic field gradient of a quadrupole magnetic field was 10 G/cm along its axis, producing a Zeeman shift gradient of 21 MHz/cm for the $^3P_1$ state.

Hg has 6 stable isotopes with abundances of more than 6%; 4 bosonic ($^{198}$Hg, $^{200}$Hg, $^{202}$Hg, and $^{204}$Hg) isotopes with nuclear spin $I = 0$, and 2 fermionic ($^{199}$Hg and $^{201}$Hg) isotopes with $I = 1/2$ and $3/2$, respectively. The spectra of trapped Hg isotopes are shown in Fig. 3, where the UV frequency was swept toward higher frequencies with a cutoff in the blue wing. The typical atom filling time was measured to be ~1 s for $^{202}$Hg. The trap spectra are about 10 MHz or $8\pi$ wide with asymmetries that are due to atom loading collisions limit their density. For odd isotopes (with hyperfine structure), stable MOTs were observed for the 

![FIG. 1 (color online). Energy-level diagram for Hg. The $^1S_0 - ^3P_1$ transition at 253.7 nm is used for magneto-optical trapping of the atoms. The $^1S_0 - ^3P_0$ transition at 265.6 nm serves as a clock oscillator. The "magic wavelength," $\lambda_c = 360$ nm, is the far-off resonance for the relevant transitions originating from the $^1S_0$ and $^3P_0$ levels.](image1)

![FIG. 2 (color online). Experimental setup. A 253.7 nm UV light was generated by frequency quadrupling a diode laser operated at 1014.9 nm with nearly 1 W. A 10 mW UV light was fed into a vacuum chamber to form a vapor-cell MOT with a folded beam configuration. ECLD, external-cavity laser diode; OI, optical isolator; TA, tapered amplifier; PZT: piezoelectric transducer, QWP: quarter wave plate.](image2)

![FIG. 3. Fluorescence spectrum of magneto-optically trapped Hg isotopes as a function of the laser frequency at 253.7 nm. The bars at the bottom indicate the positions of the resonances of individual isotopes. Detailed profiles are drawn using the magnified frequency scale shown at the top.](image3)
We start by determining the natural width of the clock transition. Although a single-photon $6s^21S_0-6s6p^3P_0$ transition is forbidden by the conservation of the angular momentum, hyperfine coupling with the nuclear angular momentum $I \neq 0$ opens a weak decay channel [29]. Our calculations of the hyperfine deexcitation result in the rate coefficients $A^{(199)\text{Hg}} = 1.3 \times 10^{-2}$ s$^{-1}$ and $A^{(201)\text{Hg}} = 8.8 \times 10^{-3}$ s$^{-1}$. In even isotopes ($I = 0$), the natural linewidth would be introduced only due to highly suppressed $E1-M1$ two-photon decays.

In an optical lattice, the shift of atomic levels is proportional to the ac polarizability $\alpha(\lambda)$, and we compute it for both clock levels. They cross at the magic wavelength of $\lambda_L = 360$ nm, which agrees with the semiempirical estimates of 358 nm [15] and of 342 nm [30]. Compared to the $E1$ contribution, the higher-rank multipolar ac polarizabilities are suppressed, and they merely shift $\lambda_L$ by a small fraction.

In addition to the dominant scalar contribution, the fermionic isotopes ($I \neq 0$) acquire vector $\alpha^{(0)}(\lambda_L)$ (and tensor for $I > 1/2$) components of the ac polarizability. The nonscalar contributions are suppressed by the ratio of the hyperfine interaction to atomic energy. The $3P_0$ level is affected the most due to the nearby levels of the $3P_j$ fine-structure manifold. We find $\alpha^{(0)}(\lambda_L) = 0.040$ a.u. for $^{199}\text{Hg}$ and $\alpha^{(0)}(\lambda_L) = -0.045$ a.u. for $^{201}\text{Hg}$.

Since the vector light shift is proportional to the $m_F$ of the Zeeman sublevels, alternating measurements of $f_{\pm}$ of the $1S_0(\pm m_F)-3P_0(F, \pm m_F)$ transition frequencies and taking the average $f_0 = (f_+ + f_-)/2$ can significantly reduce the fractional contribution $\rho$ of the vector light shift down to $\delta \nu_v = \nu_v \rho^2$, where $\nu_v = 50$ kHz is the lattice trapping frequency for the $10E_R$-deep lattice. By applying nearly linearly polarized light with an ellipticity of less than $10^{-2}$, $\delta \nu_v \sim 10^{-5}$ Hz makes a negligible contribution to our goal accuracy.

We also made a semiempirical estimate of the second-order (in the lattice intensity $I_L$) corrections to the ac Stark shift of the clock frequency $\delta \nu_h = \text{Re}(\beta I_L^2)$, where $\beta = (\gamma_{S_0} - \gamma_{P_0})/64$ is the difference between the clock-level hyperpolarizabilities and $\text{Re}(\beta)$ denotes its real part. The calculations in the single-electron approximation, as carried out in Sr [8], infer that $\gamma_{S_0}$ is about $10^2$ times larger than $\gamma_{P_0}$ at $\lambda_L = 360$ nm. It becomes smaller with decreasing $\lambda_L$ and crosses zero near 347 nm for a linear polarization. Numerically, $\beta = -(103 + 5.5i)$ mHz/(MW/cm$^2$)$^2$ for $\lambda_L = 360$ nm, and $\beta = -(21.7 + 1.5i)$ mHz/(MW/cm$^2$)$^2$ for $\lambda_L = 351$ nm. The imaginary part of $\beta$ determines the two-photon ionization rate $P_{2ph} = -4\pi \text{Im}(\beta I_L^2)$. For $I_L = 50$ kW/cm$^2$ and the linear polarization, the induced shift $\delta \nu_h$ is below 0.3 mHz, and the two-photon ionization rate does not exceed $2 \times 10^{-4}$ s$^{-1}$, which is smaller than the off-resonant (single-) photon scattering rate of $5 \times 10^{-2}$ s$^{-1}$ of the lattice lasers. For circular polarization, both the real and the imaginary part of $\beta$ are several times larger.
without any node in the indicated region of wavelengths. These second-order corrections are sensitive to both correlations and the magic wavelength of $\lambda_1$; therefore, they ultimately need to be investigated experimentally.

The sensitivity to magnetic fields $B$ is determined by the difference in the Landé $g$-factors of the ground and excited states. We find $\delta g^{(19\text{Hg})} = -4.7 \times 10^{-4}$ and $\delta g^{(20\text{Hg})} = 1.8 \times 10^{-4}$ with the CI + MBPT calculations. While the linear Zeeman shift can be eliminated by the same averaging protocol as described previously [31], the simultaneously obtained Zeeman shift $\Delta f = f_+ - f_-$ with $\delta g$ given above provides a real-time probe of the applied magnetic field to correct the second-order Zeeman effects of $\delta \nu^{(2)}_Z = -\beta_2 B^2$ with $\beta_2 = 24.4 \text{ mHz/G}^2$.

Finally, at room temperature, the accuracy of the clock is affected by blackbody radiation (BBR). The induced shift of the clock transition frequency, $\delta \omega_{\text{BBR}} = -\frac{2}{3} \times (\alpha \pi)^3 T^4 (\alpha \nu_0 - \alpha_1 S_0)$, depends on the difference in the static polarizabilities of the clock states. Our CI + MBPT calculations result in $\alpha_1 S_0 = 54.6 \text{ a.u.}$ and $\alpha_1 S_1 = 33.6 \text{ a.u.}$, leading to the BBR shift of $\delta \nu_{\text{BBR}} \approx -0.181 \text{ Hz at } T = 300 \text{ K}$. It is noteworthy that the fractional correction $\delta \nu_{\text{BBR}} / \nu_0 \approx -1.60 \times 10^{-16}$ is an order of magnitude smaller than the Sr- and Yb-based clocks [10]. Assuming a temperature uncertainty of 0.1 K, the fractional uncertainty due to the BBR is $2 \times 10^{-19}$.

In conclusion, we have demonstrated magneto-optical trapping of six isotopes of the Hg atom, the heaviest non-radioactive atom trapped so far. We have shown that Hg is a promising candidate for highly accurate optical lattice clocks with an estimated inaccuracy of less than $10^{-18}$, which is mainly limited by hyperpolarizability effects, higher-rank multipolar polarizabilities, and BBR shifts. Although currently the performance of optical lattice clocks has been investigated only at the $10^{-15}$ level [31–33], limited by the uncertainty of Cs reference clocks, a highly accurate and stable Hg-based clock will provide a new avenue for improved systematic studies of optical lattice clocks, such as the precise determination of the magic wavelength and other properties beyond the $1 \times 10^{-15}$ uncertainty level. Furthermore, because of its high Z, Hg may allow a sensitive search of the temporal variation of $\alpha$ combined with other optical clocks, e.g., Sr-based clocks, as a possible anchor [15].

We would like to thank Y. Tanino and S. I. Marmo. This work was supported in part by SCOPE, NSF, RFBR (Grants No. 07-02-00210-a and No. 07-02-00279-a), CRDF, MinES, and St. Petersburg State Scientific Center.
